

Worksheet: Calculus of Exponential and Logarithmic Functions

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1. Determine the derivative for each of the following and make any obvious simplifications.

a)  $f(x) = x^4 e^{\sin(2x)}$

b)  $f(x) = \csc(x^3 e^x)$

c)  $f(x) = \sqrt{\sec(6^x)}$

d)  $f(x) = 10^{\cos(7x)}$

e)  $f(x) = \left( \frac{e^{2x} - 1}{e^{2x} + 1} \right)^4$

f)  $f(x) = \ln[(2x+7)^7(3x+9)^9]$

g)  $f(x) = e^{\frac{x}{4-x^2}}$

h)  $f(x) = 5^{\tan x} \ln(\sec(4x))$

i)  $f(x) = \cos(e^{x^4})$

$$\text{j) } f(x) = \ln\left(\frac{3^x + 1}{3^x - 1}\right)^5$$

$$\text{k) } y = \log_4(\sin(e^{2x}))$$

$$\text{l) } y = 5^{x^3} \log(x^4)$$

m)  $y = \log_3 \sqrt{x^5 + x^2}$

2. Determine  $\frac{dy}{dx}$  for each of the following:

a)  $y = \frac{(2x-1)^4}{(x^3+1)^5 \sqrt{8x^2+1}}$

b)  $y = x^{\cos x}$

c)  $y = (\sin x)^{\sin x}$

3. Find the equation of the tangent line to the curve  $2x - y \ln y = 4$  at the point  $(2,1)$ .

4. Find the equation of the normal line to the curve  $y = \ln(e^x + e^{2x})$  at the point  $(0, \ln 2)$